

Правило преобразования:

$$(x_1) \Leftrightarrow (x_1 \vee \bar{y}_1 \vee \bar{y}_2) (x_1 \vee \bar{y}_1 \vee y_2) (x_1 \vee y_1 \vee \bar{y}_2) (x_1 \vee y_1 \vee y_2)$$

$$(x_1 \vee x_2) \Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_k) (y_k \vee x_1 \vee x_2)$$

$$(x_1 \vee x_2 \vee x_3) \Leftrightarrow (x_1 \vee x_2 \vee x_3)$$

$$(x_1 \vee x_2 \vee x_3 \vee x_4) \Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_k) (y_k \vee x_3 \vee x_4)$$

$$(x_1 \vee x_2 \vee x_3 \vee x_4 \vee x_5) \Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_k) (y_k \vee x_3 \vee \bar{y}_{k+1}) (y_{k+1} \vee x_4 \vee x_5)$$

$$(x_1 \vee x_2 \vee x_3 \vee x_4 \vee x_5 \vee x_6) \Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_k) (y_k \vee x_3 \vee \bar{y}_{k+1}) (y_{k+1} \vee x_4 \vee \bar{y}_{k+2}) (y_{k+2} \vee x_5 \vee x_6)$$

$$(x_1 \vee x_2) (x_3 \vee x_4) \Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_k) (y_k \vee x_1 \vee x_2) (x_3 \vee x_4 \vee \bar{y}_{k+1}) (y_{k+1} \vee x_3 \vee x_4)$$

Пример:

Преобразуем КНФ:

$$(x_1 \vee x_2) (x_1 \vee \bar{x}_2 \vee x_3 \vee \bar{x}_4) (\bar{x}_1 \vee x_2 \vee \bar{x}_3 \vee x_4 \vee \bar{x}_5) \Leftrightarrow$$

$$\Leftrightarrow (x_1 \vee x_2 \vee \bar{y}_1) (x_1 \vee x_2 \vee y_1) (x_1 \vee \bar{x}_2 \vee \bar{y}_2) (y_2 \vee x_3 \vee \bar{x}_4) (\bar{x}_1 \vee x_2 \vee \bar{y}_3) \dots$$

$$\dots (y_3 \vee \bar{x}_3 \vee \bar{y}_4) (y_4 \vee x_4 \vee \bar{x}_5)$$

Задача 1:

Преобразуем КНФ:

$$(x_1 \vee \bar{x}_2) (\bar{x}_1 \vee x_2 \vee x_3 \vee x_4 \vee \bar{x}_5) \Leftrightarrow (x_1 \vee \bar{x}_2 \vee \bar{y}_1) (y_1 \vee x_1 \vee \bar{x}_2) (\bar{x}_1 \vee x_2 \vee \bar{y}_2).$$

$$\bullet (y_2 \vee x_3 \vee x_4) (y_3 \vee x_4 \vee \bar{x}_5)$$

Задача 2:

Преобразуем КНФ:

$$(x_1 \vee \bar{x}_2 \vee x_3 \vee x_4) (\bar{x}_1 \vee x_2 \vee \bar{x}_3 \vee \bar{x}_4) = (x_1 \vee \bar{x}_2 \vee \bar{y}_1) (y_1 \vee x_3 \vee x_4) (\bar{x}_1 \vee x_2 \vee \bar{y}_2) (y_2 \vee \bar{x}_3 \vee \bar{x}_4)$$

Zadacha 3:

Преобразуем КНФ:

$$(x_1 \vee x_2)(\bar{x}_1 \vee x_2 \vee \bar{x}_3)(\bar{x}_1 \vee \bar{x}_2 \vee x_3 \vee \bar{x}_4 \vee \bar{x}_5 \vee x_6) = (x_1 \vee x_2 \vee \bar{y}_1)(y_1 \vee x_1 \vee x_2)(\bar{x}_1 \vee x_2 \vee \bar{x}_3) \bullet$$

$$\bullet (\bar{x}_1 \vee x_2 \vee \bar{y}_2)(y_2 \vee x_3 \vee \bar{y}_3)(y_3 \vee \bar{x}_4 \vee \bar{y}_4)(y_4 \vee \bar{x}_5 \vee x_6)$$

Zadacha 4:

Преобразуем КНФ:

$$\bar{x}_4(\bar{x}_1 \vee x_2 \vee \bar{x}_3 \vee x_4 \vee x_5 \vee x_6 \vee x_7) = (\bar{x}_4 \vee \bar{y}_1 \vee \bar{y}_2)(\bar{x}_4 \vee \bar{y}_1 \vee y_2)(\bar{x}_4 \vee y_1 \vee \bar{y}_2)(\bar{x}_4 \vee y_1 \vee y_2) \bullet$$

$$\bullet (\bar{x}_1 \vee x_2 \vee \bar{y}_3)(y_3 \vee \bar{x}_3 \vee \bar{y}_4)(y_4 \vee x_4 \vee \bar{y}_5)(y_5 \vee x_5 \vee \bar{y}_6)(y_6 \vee x_6 \vee x_7)$$

Zadacha 5:

Преобразуем КНФ:

$$(x_1 \vee x_3)(x_1 \vee \bar{x}_2)(x_2 \vee \bar{x}_3)(\bar{x}_1 \vee \bar{x}_2 \vee x_3) = (x_1 \vee x_3 \vee \bar{y}_1)(x_1 \vee x_3 \vee y_1)(x_1 \vee \bar{x}_2 \vee \bar{y}_2)(x_1 \vee \bar{x}_2 \vee y_2) \bullet$$

$$\bullet (x_2 \vee \bar{x}_3 \vee \bar{y}_3)(x_2 \vee \bar{x}_3 \vee y_3)(\bar{x}_1 \vee \bar{x}_2 \vee x_3)$$